SUBJECT USSR/MATHEMATICS/Theory of functions

CARD 1/3 PG -453

AUTHOR

GERONINUS Ja.L.

TICLE

On some properties of analytic functions being continuous in

the closed circle or sector of a circle.

PERIODICAL

Mat.Sbornik, n. Ser. 38, 319-330 (1956)

reviewed 12/1956

The paper contains some generalizations of known results of Hardy, Littlewood, Gagua and others. Let $\varphi(z) = \varphi(r e^{i\theta})$ be continuous for $r \le 1$. Let its modul of continuity for r = 1 be $\omega(\delta, \varphi) = \sup |\varphi(e^{i\theta_1}) - \varphi(e^{i\theta_2})|$, $|\theta_1 - \theta_2| \le \delta$.

Let \bigwedge be the function class for which $\int_{a}^{b} \frac{\omega(x, \Psi)}{x} dx < \infty$. If $u(\theta) \in L(0, 2\pi)$

is a real 2N-periodic function and v(0) is conjugated to it, then f(z) denotes the analytic function

$$f(z) = f(r e^{i\varphi}) = \frac{1}{2\pi} \int_{0}^{2\pi} \frac{e^{i\theta} + z}{e^{i\theta} - z} u(0) d\theta + iC,$$

The following theorems are proved:

Mat.Sbornik, n. Ser. 38, 319-330 (1956)

CARD 2/3

PG - 453

i. Let w = f(z) map the unit circle onto a region B which is bounded by a closed smooth Jordan curve C. Let $\theta(s) \in \Lambda$, where θ is the angle between the real axis and the tangent on C in the point with the arc coordinate s. Then the modul of continuity $\omega_0(\delta)$ of the functions f'(z) and f''(z) on |z|=1

satisfies the inequation

es the inequation
$$\omega_0(\delta) \leq c_1 \int_{-\infty}^{\infty} \frac{\omega(x,\theta)}{x} dx + c_2 \delta \int_{-\infty}^{\infty} \frac{\omega(x,\theta)}{x^2} dx + c_3 \omega(\delta,\theta).$$

 $\underline{2.}$ Let f(z) be regular in |z|<1, continuous in $|z|\leqslant 1$ and have a modul of continuity $\omega(\delta)=\omega(\delta,f)$ on |z|=1. Then in |z|<1 holds

$$|f'(r e^{i\varphi})| \leq c \frac{\omega[(1-r)\lg\frac{b}{1-r}]}{1-r}$$
, $r < 1$, $b > 1$.

3. If f(z) is regular in |z|<1 and if it has the modul of continuity $\omega\left(\delta\right)$ on the circular radii, then

CIA-RDP86-00513R000514910016-4

Mat.Sbornik, n. Ser. 38, 319-330 (1996)

$$|f'(r e^{i\varphi})| \le c\Omega(\frac{1}{1-r})$$

$$|f'(r e^{i\varphi})| \leq c\Omega(\frac{1}{1-r})$$
 $\Omega(x) = \int_{1}^{x} \omega(\frac{1}{x}) dx$

4. If $u(\theta) \in L(0,2\pi)$ is a real 2π -periodic function which is continuous for $\theta \in l \subset [0,2\pi]$ and if there exists the integral

$$\int_{a}^{a} \frac{\omega(x \lg \frac{b}{x}; u)}{x} dx < \infty \qquad b > 2,$$

then inside of the sector S $(r \le 1, \theta \in I)$ the inequation

$$\left|f'(r e^{i\varphi})\right| \leq c \frac{\omega\left[(1-r)\lg\frac{b}{1-r}; u\right]}{1-r}, r < 1$$

is valid.

INSTITUTION: Charkov.

CIA-RDP86-00513R000514910016-4

SUBJECT

USSR/MATHEMATICS/Fourier series

CARD 1/1

AUTHOR

GERONIMUS Ya.L.

PG - 646

TITLE

HER BEH

On some sufficient conditions for the convergence of the

Fourier-Cebysev processes.

PERIODICAL

Doklady Akad. Nauk 110, 907-909 (1956)

reviewed 3/1957

 $C \in U \cap W_I \cap U \cap Y_{I \cap I}$

Let the function f(x) be defined on [-1,+1] and the polynomials $\{p_n(x)\}_0^{\infty}$ on the same interval be orthogonal with respect to $d\,\psi(x)$ and normalized. In a table the author establishes nine sufficient conditions for the convergence of the Fourier-Cebysev process

$$\lim_{n\to\infty} S_n(f;x) = \sum_{k=0}^{\infty} a_k p_k(x) = f(x), \quad a_k = \int_{-1}^{+1} f(x) p_k(x) d \psi(x) \quad k=0,1,....$$

The first condition relates to the quasi-uniform convergence on [a,b] (-1< a < b < +1) all other conditions guarantee a uniform convergence on [-1,+1]. The conditions are concluded from the estimations of the author (Doklady Akad. Nauk 103, No. 3 (1955)).

SOV/44-58-4-3038

Translation from: Referativnyy zhurnal, Matematika, 1958,

Nr 4, p 89 (USSR)

AUTHOR: Geronimus, Ya. L.

TITLE: On Certain Finite Difference Equations and Corresponding

Systems of Orthogonal Polynomials (O nekotorykh

uravneniyakh v konechnykh raznostyakh i sootvetstvuyushchikh

sistemakh ortogonal'nykh mnogochlenov)

PERIODICAL: Uch. zap. Khar'khovsk. un-ta, 1957, Nr 80; Zap. Matem.

otd. fiz-matem. fak. i Khar'khovsk. matem. o-va, 25.

pp 87-100

ABSTRACT: With several additions, a detailed proof is given of earlier results of the author (Dokl. AN SSSR, 1940, Nr 29,

pp 536-538). Let $\{\alpha_{\kappa}\}$ and $\{\lambda_{\kappa}\}$ ($\lambda_{\kappa}\neq 0$) be two sequences of complex numbers. Following Perron and Stieltjes, according to the given numbers a sequence of polynomials $\{P_{\kappa}^{(\ell)}(Z)\}$ is constructed, where-

Pn(1)(z) and \, Pn-1(z)

Card 1/3

SOV/44-58-4-3038

On Certain Finite Difference Equations (Cont.)

are particular solutions of the difference equations

If periodicity occurs, that is $\lambda_n y_{n-2} = 0$ (1)

an=am, In=lm, n-s=m(mod K); (m=0,1,..., k), n>s+1, s>0 (x)

then the solution of equation (1) satisfies an equation with constant coefficients

(3)

 $y_{n+2k}-(p_k-r_{k-2})y_{n+k}+ly_n=0$, $n\geq s-1$ Here P_k and r_{k-2} are certain polynomials with respect to z and $1=l_1$ $1_2\cdots l_k$.

The solution of equation (3) is found in explicit form; certain of its properties and properties of the polynomial of the form $P_k(z)$ (z) are indicated.

Card 2/3

SOV/44-58-4-3038

On Certain Finite Difference Equations (Cont.)

If all the parameters $\{a_{\gamma}\}$ and $\{\lambda_{\gamma}\}$ $(\lambda_{\gamma}>0)$ are real, then as is known, the corresponding polynomials $\{P_n(x)\}$ are orthogonal in the sense that there exists such a $d\psi(x)$ that $\int_{-\infty}^{+\infty} P_n(x) P_n(x) d\psi(x) = 0$, $m \neq h$, and they satisfy equation (1). It is shown that when the condition (2) is satisfied, $\psi(x) = \psi(x) + \psi(x)$. Function $\psi(x)$ is an absolutely continuous component, and $\psi(x)$ is a jump function. Certain properties of $\psi(x)$ and $\psi(x)$ are established. The proof is based on the study of continuous fractions. In conclusion some examples are cited. In the work of the author (Izv. AN SSSR, 1941, 5, Nr 3, pp 203-210) a more general case of limit periodicity is studied.

A.A. Mirolyubov

Card 3/3

HER FER!

CIA-RDP86-00513R000514910016-4

SOV/124-59-1-43

Translation from: Referativnyy zhurnal. Mekhanika, 1959, Nr 1, p 4 (USSR)

AUTHOR:

Geronimus, Ya.L.

TITLE:

On the Properties of the Hamilton-center of Certain Vector Systems

PERIODICAL: Tr. Khar kovsk. aviats. in-ta, 1957, Nr 17, pp 11-21

ABSTRACT:

Some new facts with reference to the properties of the Hamilton-center in application to certain special systems of stationary physical vectors are given. For example, in application to a vector-system, lying in planes perpendicular to some straight line, is proved the invariance of the Hamilton-center and of the parameter of the screw of the given system relative to the group of retations of vectors in their planes; demonstration is based upon the application of the quaternion-theory. Some results of the treatise can be applied, for example, to the research of the properties of the Hamilton system of vectors $m(d^n\pi/dt^n)$ with reference to the rotation of a body around an axis and with reference to the plane-parallel motion; the part of the Hamilton-center in applying the forces of inertia of the points of a symmetrical gyroscope in the case of regular precession is interpreted, et a.

Card 1/1

V.V. Dobronravov

GERONIMUS, Ye.L., prof., doktor fiz.-mat. nauk.

Activity of the Kharkov branch of the Seminar on the Theory of Machines and Mechanisms. Trudy Inst. mash. Sem. po teor. mash. 17 no.65:18-19 '57. (MIRA 10:12)

ere egge et fin estre coministre egge fra voir manina directif en vandade d'Astre 1919 de 1811. Le de Maistre de 1919 de 1

 Nauchnyy rukovoditel' Khar'kovskogo filiala seminara po teorii mashin i mekhanizmov Instituta mashinovedeniya AN SSSR. (Kharkov--Mechanical engineering)

GERONIMUS, Ya.L. (Khar'kov)

Certain finite-difference equations and corresponding systems of orthogonal polynomials. Uch.zap.KHGU 80:87-160 '57.

(MIRA 12:11)

(Difference equations) (Polynomials)

AUTHOR

GERONIMIS 14.L

PA - 3122

TITLE

On the Uniform Convergence of the FOURIER-CHEBYSHEV and the MACLAURIN Developments of the Analytical Functions of the Class

"2

PERIODICAL

ABSTRACT

Doklady Akademii Nauk SSSR 1957, Vol 113, Nr 3, pp 491-492 (USSR). Received: 6/1957 Reviewed: 7/1957 The polynomials $\{P_n(z)\}$ are assumed to be orthonormal in the unit surrounding $z=e^{i\theta}$ with respect to the weight $p(0)\geqslant 0$ where $l_{\mathbb{C}}p(\theta)\in L_1$ applies. The function f(z) is assumed to be regular within the domain |z|<1, where $f(z)\notin H_2$ and $f(z)/\pi(z)\in H_2$

apply. Here

 $\pi(z) = \exp\left\{-\frac{1}{4\pi} \int_{0}^{2\pi} \frac{e^{i\theta} + z}{e^{i\theta} - z} \ell_{SP}(\theta) d\theta\right\}, |z| < 1$

is denoted by $s_n(f;z)$. $\sigma_n(f;z)$ are the partial sums of the developments of the function f(z) into a FOURIER-CHEBYSHEV-series according to the orthogonal polynomials $\left\{P_k(z)\right\}$ and into a

CARD 1/4

PA - 3122

On the Uniform Convergence of the FOURIER-CHEBYSHEV and the MACLAURIN Developments of the Analytical Functions of the Class

MAC LAURIN series, i.e. according the polynomials $\left\{z^k\right\}$:

$$s_{n}(f;z) = \sum_{k=0}^{n} c_{k} P_{k}(z), c_{k} = (1/2\pi) \int_{0}^{2\pi} f(e^{i\theta}) P_{k}(e^{i\theta}) p(\theta) d\theta$$

$$\sigma_{n}(f;z) = \sum_{k=0}^{n} \gamma_{k} z^{k}, \gamma_{k} = (1/2\pi)^{2\pi} \int_{0}^{\pi} f(e^{i\theta})e^{-ik\theta}d\theta$$

f all theorems on the convergence of the FOURIER-CHEBYSHEV-developments the theorem on the uniform convergence of these decompositions is the most interesting. Here the condition is concerned, for which the limiting relation lim

CARD 2/4

 $\lim_{n\to\infty} \left\{ s_n(f;e^{i\theta}) - \sigma_n(f;e^{i\theta}) \right\} \text{ applies uniformly within a certain }$

PA - 3122

On the Uniform Convergence of the FOURIER-CHEBYSHEV and the MACLAURIN Developments of the Analytical Functions of the Class $\rm H_2^{\circ}$

section $[a,\beta]$ o $[0,2\pi]$

Theorem: The weight $p(\theta)$ is assumed to be limited in the section $[a,\beta]$ by a positive number and to be steady with the stability modulus (δ,p) .

This stability modulus satisfies the condition by DINI-LIPP-SCHITZ

 $\omega(\delta;p) \leq c(\lg(1/\delta))^{-1} \Gamma$, $\gamma > 2$

The function f(z) is assumed to have a limited radial limit value in all points of the arc. [e^{i\alpha}, e^{i\beta}].

In this case the condition $\lim_{n\to\infty} \{e_n \text{lgn} = 0 \text{ with }$

 $|P_n^*(e^{i\theta}) - \pi(e^{i\theta})| \leq \xi_n, P^*(z) = z^n P_n(1/z), \alpha + \eta \leq \theta \leq \beta - \eta.$

is sufficient for the uniform convergence of $\lim_{n\to\infty} \{s_n(f;e^{i\theta}) - \sigma_n(\hat{x}e^{i\theta})\}$

CARD 3/4

PA - 3122

On the Uniform Convergence of the FOURIER-CHEBYSHEV and the MACLAURIN Development of the Analytical Functions of the Class $\rm H_2$.

= 0 in the section $[a + \eta', \beta - \eta'], \eta' > \eta$. Thus, the existence of the asymptotic formula with the error $\{\eta^{-} 0(1/\lg n)\}$ satisfied the conditions of uniform convergence. A table contains the 5 conditions found here, each of which suffices for the existence of the here mentioned asymptotic formula. (1 Table).

ASSOCIATION: not given.

PRESENTED BY: V.I. SMIRNOW Member of the Academy, 6.10. 1956.

SUBMITTED: 4.10. 1956.

AVAILABLE: Library of Congress.

CARD 4/4

At IHOR: GERONINUS, Ya., L.. 20-1-5, 42

TITLE:

On Some Estimations in the Theory of Toplitz Forms and Orthogonal Polynomials (O nekotorykh otsenkakh v teorii form Teplitsa

i ortogonal'nykh mnogochlenov)

PERIODICAL:

Doklady Akad . Nauk SSSR.

1957, Vol. 117, Nr. 1, pp. 25-27 (USSR)

ABSTRACT:

The author considers the forms

$$T_n = \sum_{i,k=0}^{n} c_{i-k} x_i \overline{x}_k$$
, $c_{-n} = \overline{c}_n$, $\Delta_n = \left| c_{i-k} \right|_0^n$, $n=0,1,2,...$,

positive definite for $\left\{ \Delta_{n}^{\infty}\right\} >0$. If it is denoted

 $h_n = \frac{\Delta_{n+1}}{\Delta_n}$, then there exists $\lim_{n \to \infty} h_n = h \geqslant 0$.

The author gives several estimations for the magnitude /n = h - h and shows that various estimations can be ex-

pressed by μ , e.g. the estimation of increase of orthogonal polynomials. 5 Soviet and 2 foreign references are quoted.

ASSOCIATION: Khar'kov Institute of Aviation (Khar'kovskiy aviatsionnyy institut) By V.I.Smirnov, Academician, May 23, 1957

PRESENTED: SUBMITTED:

May 21, 1957

AVAILABLE:

Library of Congress

Card 1/1

Ya. L. Geroniumus, "The Application of the Tschebischew Methods in Some Problems of Dynamic Mechanism Synthesis."

paper presented at the 2nd All-Union Conf. on Fundamental Froblems in the Theory of Machines and Mechanisms, Moscow, USER, 24-28 Murch 1958.

16(1); 25(2)

PHASE I BOOK EXPLOITATION

SOV/1741

Geronimus, Yakov Lazarevich

Dinamicheskiy sintez mekhanizmov po metodu Chebysheva (Dynamic Synthesis of Mechanisms According to Chebyshev Method) Khar'kov, Izd-vo Khar'kovskogo univ., 1958. 133 p. 3,000 copies printed.

Resp. Ed.: Yu.V. Epshteyn; Ed.: D.A. Vaynberg; Tech. Ed.: Ya.T. Chernyshenko,

PURPOSE: This book is intended for senior students at vtuzes and for engineers and mathematicians.

COVERAGE: The book deals with the problem of the dynamic synthesis of mechanisms according to Chebyshev's method and the development and application of this method by Soviet mathematicians. Methods studied and results received in the book may have direct application to practical problems. The book is an extension of the author's report on the theory of machines and mechanisms presented at the meeting of the Institut mashinovedeniya (Institute

Card 1/6

Dynamic Synthesis of Mechanisms (Cont.) SOV/1741 of Mechanical Engineering) of the Academy of Sciences, USSR, held on the occasion of the 130th anniversary of Chebyshev's birth. Contemporary Soviet scientists mentioned in connection with the problem presented in the book include Academician V.A. Steklov, Academician I.I. Artobolevskiy, N.I. Levitskiy, Z.Sh. Blokh, V.I. Ivanov, P.N. Gartshtein, Yu. V. Epshtein, L.I. Shteyuvol'f, and L.B. Geyler. There are 53 references, of which 52 are Soviet and 1 French. TABLE OF CONTENTS: Preface 3 Ch. I. Chebyshev's Problem Concerning Approximate Isochronal Regulator 1. Statement of problem and derivation of basic equation 9 2. Chebyshev's first method for the solution of the 12 problem 3. Chebyshev's correction method
4. Concepts of polynomials with the least deviation 17 18 from zero Card 2/6

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PHASE I BOOK EXPLOITATION

501/1642

Geronimus, Yakov Lazarevich

Mnogochleny, ortogonal nyye na okruzhnosti i na otrezke; otsenki, asimptoticheskiye formuly, ortogonal nyye ryady (Polynomials Which Are Orthogonal on
a Circle and on a Segment; Estimates, Asymptotic Formulas, Orthogonal Series)
Moscow, Fizmatgiz, 1958. 240 p. (Series: Sovremennyye problemy matematiki)
5,000 copies printed.

Ed.: V. S. Videnskiy; Tech. Ed.: V. N. Kryuchkova.

PURPOSE: This book may be useful to scientific workers and Aspirants working in mathematics or mathematical physics.

COVERAGE: The book presents the author's attempt to develop and to apply the methods and ideas of Soviet mathematicians V. A. Steklov, S. N. Bernshtein, V. I. Smirnov, A. N. Kolmogorov, N. I. Akhiyezer, M. G. Kreyn and of such

Card 1/5

 Polynomials Which Are Orthogonal (Cont.)

SOV/1642

non-Soviet mathematicians as G. Szegő, P. Erdős, P. Turan and G. Freud to the solution of important problems of the theory of orthogonal polynomials. The author deals with those properties of orthogonal polynomials, on which the convergence of infinite processes connected with orthogonal polynomials depends - the Fourier-Chebyshev process, the interpolation process with nodes in zeros of orthogonal polynomials, etc. The monograph gives a systematic presentation of the works of Soviet and non-Soviet mathematicians, including the author, in this field of mathematics. The book is one of a series published by the editorial staff of Uspekhi matematicheskikh nauk. The author thanks N. I. Akhiyezer for reading the manuscript and for valuable remarks. There are 67 references, of which 36 are Soviet, 14 English, 10 German, 6 French and 1 Czech.

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507/140-58-1-3/21 Geronimus, Ya.L. (Kharkov) AUTHOR: On Some Properties of the Functions of the Class L_n (O nekoto-TITLE: rykh svoystvakh funktsiy klassa Ln) Izvestiya vysshikh uchebnykh zavedeniy Ministerstva vysshego PERIODICAL: obrazovaniya SSSR, Matematika, 1958, Nr 1 pp 24-32 (USSR) Let f(0) be a real 27 -periodic function of the class L, ,p) 1 ABSTRACT: and $\omega_{p}(\delta,f) = \sup_{|h| \leq \delta} \|f(\theta+h) - f(\theta)\|_{p}$, $\lim_{\delta \to 0} \omega_{p}(\delta,f) = 0$. The author proves the theorem already announced in [Ref 2] and the following further theorems: Theorem: Let $f(\theta) \in L_p, p > 1$, $\sum_{n=1}^{\infty} n^{-1/p} \omega_p \left(\frac{1}{n} ; f\right) < \infty$, $\frac{1}{p} + \frac{1}{p}$, = 1 Then $f(\theta)$ is equivalent to a continuous function $f_{0}(\theta)$ with the dulus of continuity $\omega(\delta, f_0) \leqslant C \sum_{1/F}^{\infty} \frac{dx}{x} \int_{x}^{\infty} y^{-1/p^{1}} \omega_{p} \left(\frac{1}{y}; f\right) dy$ Card 1/3

307/140-58-1-3/21 On Some Properties of the Functions of the Class L

(so far as the double integral exists).

Theorem: If
$$f(\theta) \in L_p$$
, $p > 1$ and $\omega_p(\delta, f) = 0 \left\{ \delta^{1/p} \left[\lg \frac{1}{\delta} \right]^{-3} \right\}$

then the Fourier series of $f(\theta)$ converges uniformly on $[0,2^{\frac{11}{11}}]$ and attains almost everywhere the values of $f(\theta)$. Theorem: Let $f(\theta) \in L_1(0,2\pi)$, on $[\mathcal{L},\beta] \subset [0,2\pi]$ let

 $f(\theta) \in L_p$, p > 1 and

$$\omega_{p}'(\delta; f) = \sup_{|h| \le \delta} \left\{ \frac{1}{2\pi} \int_{0}^{\beta} |f(\theta + h) - f(\theta)|^{p} d\theta \right\}^{1/p} = 0 \left\{ \int_{0}^{1/p} \left[\log \frac{1}{p} \right]^{-3} \right\}$$

Then the Fourier series of f(0) converges uniformly in [4,8] and attains almost everywhere the values of f(0) -Some further results related to the results of Hardy and Littlewood are given.

There are 12 references, 5 of which are Soviet, 1 Polish, 1 English, 1 French, 1 Hungarian, 1 American, and 2 German.

Card 2/3

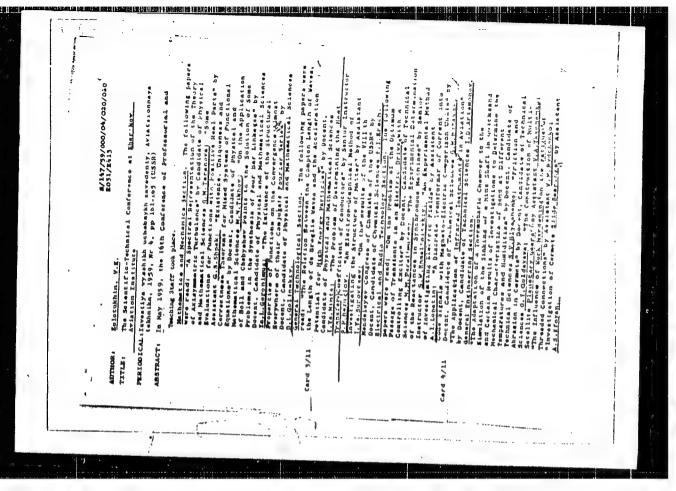
On Some Properties of the Functions of the Class L p SOV/140-58-1-3/21

ASSOCIATION: khar'kovskiy aviatsionnyy institut (Khar'kov Aviation Institute)

SUBMITTED: September 23, 1957

Card 3/3

Some ev skolv:	valuations for orthogonal polynomials. Nauch. dokl. v fizmat.nauki no.1:28-31 '58. (MIRA 12:	ув.
	'kovskiy aviatsionnyy institut.	3)
	(Functions, Orthogonal)	



24.4100

3/044/62/000/009/004/069 A060/1000

AUTHOR:

Geronimus, Ya. L.

TITLE:

On some methods of constructing Burmester curves and points. I.

PERIODICAL:

Referativnyy zhurnal, Matematika, no. 9, 1962, 65, abstract 9A366 ("Bul. Inst. politehn. Iași.", 1959, V, (IX), no. 3 - 4, 234 - 254

(Summaries in English, Rumanian))

TEXT: In the theory of mechanisms, Burmester's curves are the curves of circular points and the curve of centers. The former is characterized by the equation $(x^2 + y^2)$ (mx + ly) - lm xy = 0, and the latter by a similar equation, but with the parameter 1 replaced by 1', defined by the equality: 1/1 - 1/1' = = 1/d, where d is the diameter of the winding curve. The double point of each of these curves coincides with the instantaneous center of velocities. Here the first part considers the transformation of Burmester's curves into a straight line, an equilateral hyperbola, a circle, and a parabola, using projective methods. Geometrical methods of constructing Furmester's curves are given: 1) given the coordinate axes and two points, 2) given two points, the focal axis and a Card 1/2

67. .: 16(1)-11 41 1. 46.1. AUTHOR: Ceronimus Ya.L. \$07/20-129-4-3/68 TITLE: On the Order of Approximation by Means of Poisson's Integral, PERIODICAL: Doklady Akademii nauk SSSR, 1959, Vol 129, Nr 4, pp 726-728 (USSR) ABSTRACT: Let $f(\theta) \in L(0,2\pi)$ be a complex-valued, 2N-periodic function of the real argument 0, $0 \le 9 \le 2\pi$. Let furthermore (1) $F(re^{i\varphi}) = \frac{1}{2\pi} \int_{0}^{\pi} f(\theta) P(r, \theta - \varphi) d\theta$, $P(r, t) = \frac{1 - r^2}{1 - 2r \cos t + r^2}$, r < 1and (2) $\Delta(r, \varphi) = F(re^{i\varphi}) - f(\varphi) = \frac{1}{2\pi} \int_{w} \varphi(t) F(r, t) dt$, r < 1, where $w_{\varphi}(t) = f(p+t)+f(p-t)-2f(\varphi)$. Let $f(\theta)$ be continuous in Ψ or let it have there a discontinuity of first kind; let (4) $f(\psi) = \frac{1}{2} \{ f(\psi+0) + f(\psi-0) \}$ and $\psi_{\varphi}(\delta) = \sup_{|t| \le \delta} |\psi_{\varphi}(t)|.$ (5) Theorem 1: If for a $\chi(0<\chi\leq 1)$ there exists the integral Card 1/3

On the Order of Approximation by Means of Poisson's 507/20-129-4-3/68 Integral

(6)
$$\int_{0}^{\pi} |w_{\varphi}(t)| t^{-1-r} dt,$$

then for $r_0 \leqslant r \leqslant 1$ there holds the inequation

(7)
$$|\Delta(r,\varphi)| \leq C(1-r)^{\gamma} \int_{0}^{\pi} |w_{\varphi}(t)| t^{-1-\gamma} dt, \quad C = \frac{1}{\pi} \left(\frac{\pi^{2}}{4r_{0}}\right)^{\frac{1+\gamma^{2}}{2}}$$

Theorem 2: For ro≤r<1 it holds

(9)
$$|\Delta(r,\varphi)| \leq c_2 \frac{1-r}{6^2}$$
, $c_2 = \frac{\pi}{4r_0} \left\{ \int |f(t)| dt + 2\pi |f(\varphi)| \right\} + 1$

Where δ is determined

where δ is determined from

(10)
$$1-r^2 = \delta^2 W_{10}(\delta)$$

(10) $1-r^2 = \delta^2 W_{\phi}(\delta)$. Further 4 theorems contain estimations for $|\Delta(r,\phi)|$ in other cases, especially if the behavior of the function on a set $E \subset [0,2\pi]$ is known, e.g.:

Card 2/3

On the Order of Approximation by Means of Poisson's SOV/20-129-4-3/68

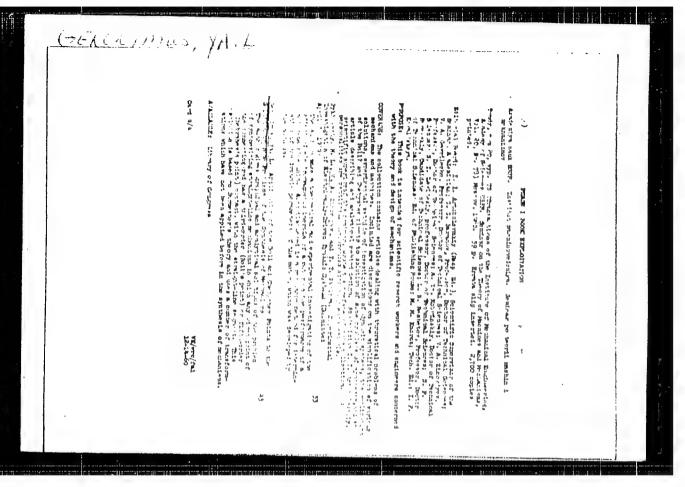
Theorem 5: Let f(θ) be continuous on [α,β] C [0,2π] and let it have there the modulus of continuity ω(δ). Then for α+εςγ, ψ ≤ β-ε, ε>0, r < 1 there holds the estimation

(15) | Δ(r,γ)| ≤ C (1-r) + ω(|φ-ψ|) + C ω (1-r) lg 1/(1-r), where the constants C and C do not depend on r, ψ, ψ.

The author mentions I.P. Natanson. There are 2 Soviet references.

PRESENTED: July 16, 1959, by S.N. Bernshteyn, Academician.

Card 3/3



S/044/62/000/009/005/069 AC6C/ACOO

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AUTHOR:

Geronimus, Ya. L.

TITLE:

On some methods of constructing Burmester curves and points. II.

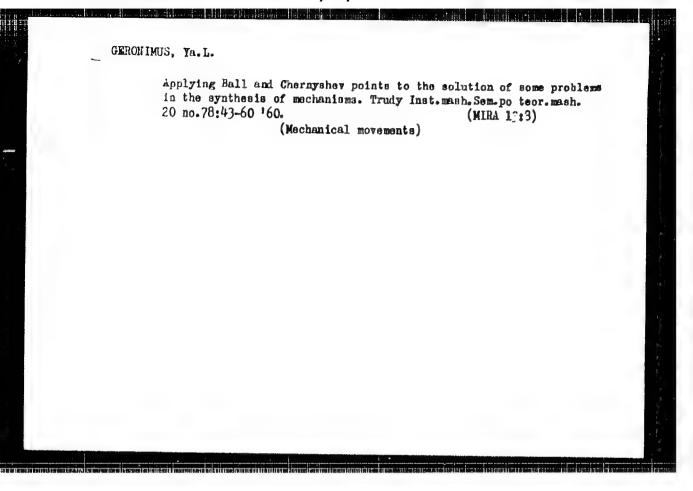
PERIODICAL:

Referativnyy zhurnal, Matematika, no. 9, 1962, 65, abstract 9A367 ("Bul. Inst. politehn. IABI", 1960, v. 6, no. 3 - 4, 275 - 290

(Summaries in English, Rumanian))

TEXT: In the author's preceding paper (abstract 9A366) the construction of one of Burmester's curves was given. The present paper considers the simultaneous construction of both curves. For a complete determination of these curves it is necessary to give four conditions for the general case. Attention is paid to the case when the conditions imposed separately upon each of the curves do not determine it, but the totality of the conditions imposed upon both curves determine the latter. For the motion of a moving plane along the fixed plane the points of the first Burmester's curve possess the property that their trajectories have at those points an osculation of an order not lower than the third with their circles of curvature; it is known that in a

Card 1/2



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80206 5/038/60/024/02/04/007

AUTHOR: Geronimus, Ya.L.

TITLE: On Gome Estimations for the Coefficients of Bounded Functions

PERIODICAT: Izvestiya Akademii nauk SSSR, Seriya matematicheskaya, 1960, Vol. 24, No. 2, pp. 203-212

TEXT: Let 3 denote the class of the functions

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 $f(z) = \sum_{k=0}^{\infty} \alpha_{k}^{2}$ which are

regular in |z| < 1 and satisfy the condition |f(z)| < 1.

Theorem 1: If
$$f(z) \in S$$
 and $\frac{3}{2} m < n \le 2m$, then it holds:
$$|\alpha_n| \le \alpha = 14\sqrt{3} - 24$$
(II) $|\alpha_n| \le \alpha = 14\sqrt{3} - 24$

(II)
$$|\alpha| \le \begin{cases} \frac{4\sqrt{3}}{8} \left\{ 1 - \frac{9}{8} |\alpha_n| + \left(1 - \frac{3}{4} |\alpha_n|\right)^{3/2} \right\}^{1/2}, |\alpha_n| \ge x \end{cases}$$

where $\mu > \frac{2}{3}$ is the root of $\mu^2 - \mu^3 = |\alpha_n|^2$. The equality sign only holds Card 1/3

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On Some localisations for the Complete of Bounded Functions

$$f^{*}(z) = \begin{cases} z^{2m-n} & \frac{\sqrt{1-\mu+z^{n-m}}}{z^{n-m}\sqrt{1-\mu+1}}, & |\alpha_{n}| \leq \alpha \\ \\ z^{2m-n} & \frac{8\lambda^{2}z^{2(n-m)}+4\lambda z^{n-m}-1}{8\lambda^{2}+4\lambda z^{n-m}-z^{2(n-m)}}, & |\alpha_{n}| \leq \alpha \end{cases}$$

Theorem 2 is the special case for m = 1, n = 2. Theorem 3: Let $f(z) \in S$. 1.) If m is the smallest value of the index n for which the inequality $|\propto_n| \leq \frac{\sqrt{5}-1}{2}$ does not hold, then this inequality can be wrong only for the values $m \leq n \leq 2m$. ?.) If m is the smallest value of a for which $|\propto_n| \leq \frac{14\sqrt{7}-20}{27}$ does not hold, then this inequality can Card 2/3

On Some Estimations for the Coefficients of Bounded Functions

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be wrong only for the values $m \le n \le \frac{3}{2} m$.

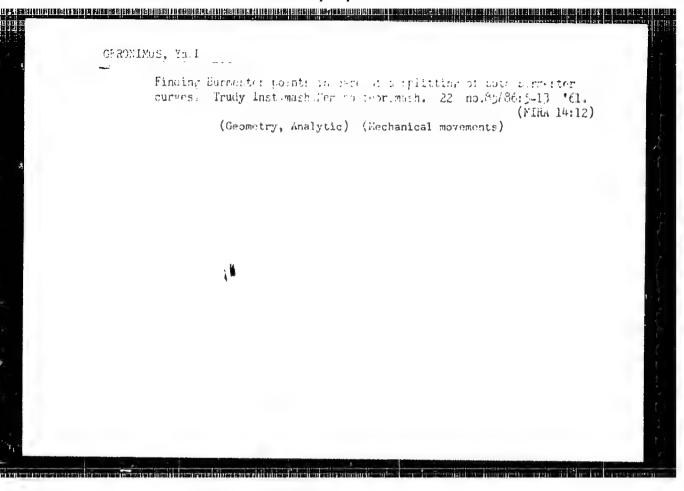
Theorem 4 is already partially contained in (Ref. 3) by G.M. Goluzin. There are 7 references: 3 Soviet, 3 Hungarian and 1 American.

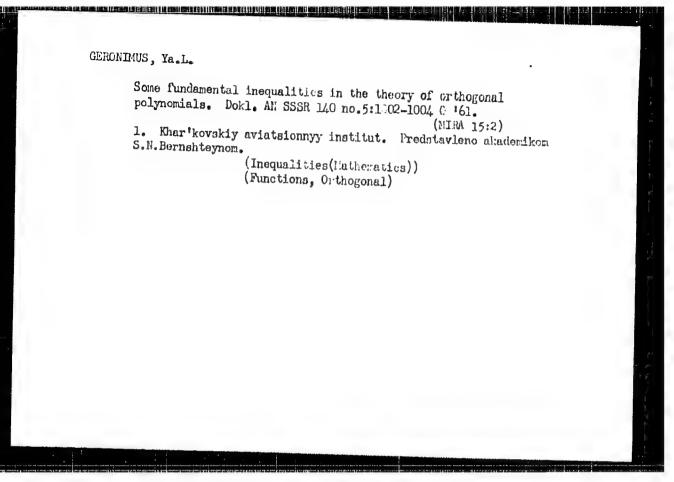
PRESENTED: by S.N. Bernshteyn, Academician

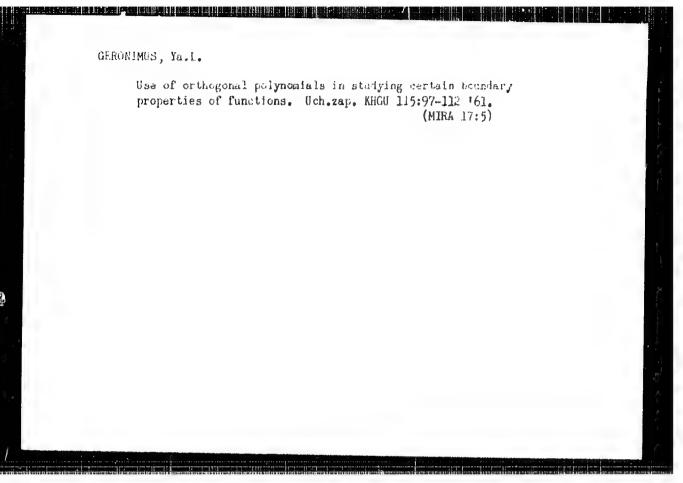
SUBMITTED: January 31, 1959

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Card 3/3







GERONIMUS, Yakov Lazarevich; SPERANSKIY, N.V., red.; MUMUNSHOVA, M.Ya., tekhn. red.

[Geometrical apparatus of the theory of synthesis of plane mechanisms]Geometricheskt apparat teorii sinteza ploskikh nekhanizmov. Moskva, Fizmatgiz, 1962. 399 p. (MIRA 15:11)

(Geometry, Modern) (Machanics, Analytic)

9,3140

31942 \$/057/62/032/001/001/018 B146/B112

AUTHOR:

Geronimus, Ya. L.

DEFENDENCE OF THE REPORT OF THE RESEARCH CONTROL OF TH

TITLE:

Methods of producing fields with focusing properties

PERIODICAL: Zhurnal tek nicheskoy fiziki, v. 32, no. 1, 1962, 3-14

TEXT: The author studied the motion of charged particles in a steady electromagnetic field; he describes methods of finding focusing fields in some special cases. The interaction between particles is neglected, and particle motion is considered in two-dimensional approximation. The Hamilton-Jacobian differential equation referred to orthogonal,

curvilinear, isothermal coordinates q_1 , $q_2(ds^2 = \sigma^2(dq_1^2 + dq_2^2))$

$$\left(\frac{\partial \overline{W}}{\partial q_1} - \frac{e_0 a A_1}{c}\right)^2 + \left(\frac{\partial \overline{W}}{\partial q_2} - \frac{e_0 a A_2}{c}\right)^2 = v^2, \tag{1.3}$$

$$v^2 = v^2 (q_1, q_2) = 2m_0 r^2 \left\{ h - e_0 \varphi + \frac{1}{2m_0 c^2} (h - e_0 \varphi)^2 \right\},$$

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Methods of producing fields with ...

 $(m_0 - mass at rest, h - total energy, e_0 - charge, v - p rticle velocity;$ A1, A2 - vector potential components) is integrated for the special case of a cyclic coordinate. One obtains the particle orbits, the focusing condition and, finally, the required electromagnetic field. It is shown that the integration variable in the focusing condition cannot be monotonically growing; cases are considered where it has one or two extreme values. The absence of the electric field and the case of constant v^2 for the variable with one extreme value, the case v^2 = const., and v = su (0 s 1, u - function of the coordinate) for the variable with two maxima are specially dealt with. A paper by P. P. Pavinskiy (Ref. 2: Izv. Al. SSSR, ser. fizich., 18, no. 2, 175, 1954) is mentioned. There are 4 figures and 7 references: 5 Soviet and 2 non-Soviet.

ASSOCI TION: Khar'kovskiy aviatsionnyy institut (Khar'kov Aviation

Institute)

SUB.AITTED: Hovember 25, 1960

Card 2/

S/057/62/032/007/008/013 B104/B102

NUTHOR:

Geronimus, Ya. L.

TITLE:

Focusing fields

PERIODICAL: Zhurnal tekhnicheskoy fiziki, v. 32, no. 7, 1962, 848-858

TEXT: The motion of a material point in a focusing potential field is investigated. The Hamilton-Jakobi equation in curvilinear orthogonal coordinates \mathbf{q}_4 and \mathbf{q}_2 reads:

$$\frac{1}{2m} \left\{ \frac{1}{h_1^2} \left(\frac{\partial W}{\partial q_1} \right)^3 + \frac{1}{h_2^2} \left(\frac{\partial W}{\partial q_2} \right)^2 \right\} + V = h, \quad V = V(q_1, q_2). \tag{1.2}$$

To solve the equation, the coordinates are assumed to be isothermal: $n_1 = h_2 = \sigma(q_1, q_2)$; further, it is assumed that

 $\sigma^2(q_1,q_2) = a_1(q_1) + a_2(q_2)$, where a_1 and a_2 are known functions. For the potential, it is assumed: $V = [b_1(q_1) + b_2(q_2)]/[a_1(q_1) + a_2(q_2)]$,

Card 1/2

Focusing fields

S/057/62/032/007/008/013 B104/B102

where $b_1(q_1)$ and $b_2(q_2)$ are the desired functions. On these assumptions, a total integral of (1.2) is obtained with the aid of Liouville's theorem. The condition for focusing is derived from the condition for the trajectories:

$$\int\limits_{q_{10}}^{q_{1}^{*}} \frac{dq_{1}}{\sqrt{2mha_{1}\left(q_{1}\right)-b_{1}\left(q_{1}\right)+\gamma}} = \int\limits_{q_{10}}^{q_{1}^{*}} \frac{dq_{2}}{\sqrt{2mha_{2}\left(q_{2}\right)-b_{2}\left(q_{2}\right)-\gamma}} \, ,$$

wherein \mathbf{q}_1 and \mathbf{q}_2 are the end points, \mathbf{q}_{10} and \mathbf{q}_{20} are the starting points of the trajectories, $\gamma_1\leqslant\gamma\leqslant\gamma_2$ holds for the arbitrary constant γ . The focusing problem is solved for one and for two extreme values of \mathbf{q}_2 . Finally, a geometrical solution method according to Euler-Maupert is examined. There are 4 figures.

AGGOCIATION: Khar'kovskiy aviatsionnyy institut (Khar'kov Aviation

Institute)

SUBMITTED: August 12, 1961

Card 2/2

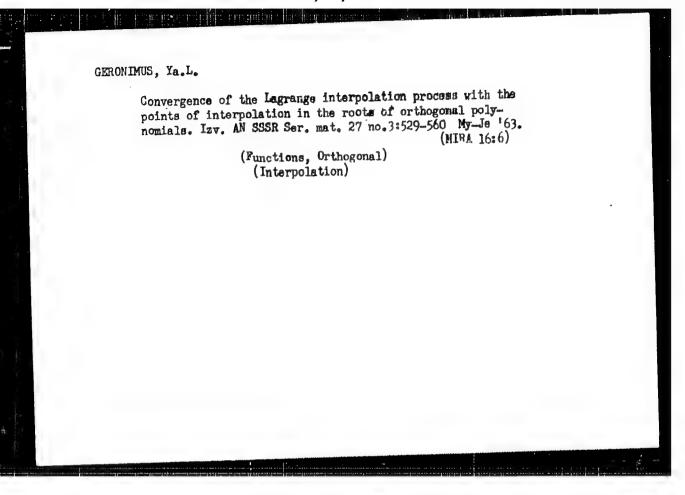
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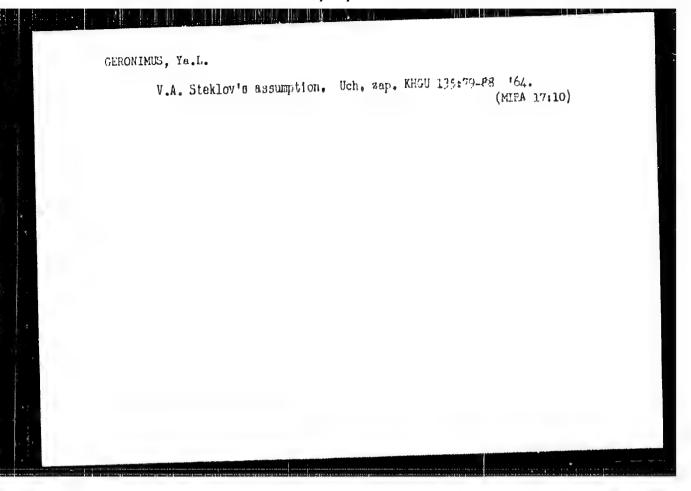
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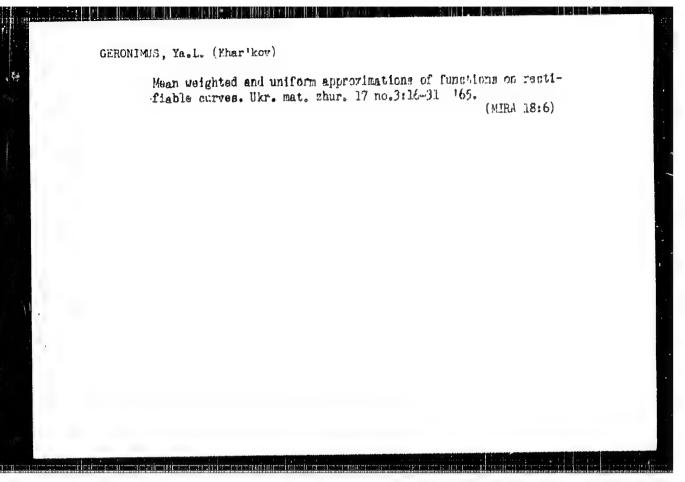
1. khar'kovskiy aviatsionnyv institut. Preustavleno akademikom S.N.Bernshteynom. (Polynomials)

GERONIMUS, Ya.L. Relation between the order of growth of orthonormal polynomials and the nature of distribution. Dokl. AN SSSR 146 no.2:281-283 s 162. 1. Khar'kovskiy aviatsionnyy institut. Predstavleno akademikom S.N. Bernshteynom. (Polynomials)

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GERONIMES, Ye.L. (Enserteer)

Some imbrediag theorems. Inv.vyc.ucheb.nav.; rat. no.6:
62-62 *65. (ETA 19:1)

1. Submitted May 25, 1964.

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SOURCE CODE: UR/0420/65/000/003/0003/0013

AUTHOR: Geronimus, Ya. L. (Professor)

11

ORG: none

TITLE: Several forms of equations of motion for a material system with nonholonomic nonlinear couplings

SOURCE: Samoletostroyeniye i tekhnika vozdushnogo flota, no. 3, 1965, 3-13

TOPIC TAGS: motion equation, motion mechanics, theoretical mechanics

ABSTRACT: Most literature on analytical and theoretical mechanics considers material systems with holonomic or nonholonomic linear coupling. Only in the derivation of the Gauss minimum principle has it been shown that it holds for nonholonomic, nonlinear coupling. Since this principle is equivalent to the Appel' equations, the question of why the latter hold only for linear nonholonomic coupling remains unresolved. The present paper deals with several forms of equations of motion for systems with nonlinear, nonholonomic coupling. These are obtained by considering the virtual displacement of points (as demonstrated by M. V. Ostrogradskiy, no reference) at fixed configurations and velocities (as is normally done in the derivation of the Gauss principle). For a system with nonholonomic, nonlinear coupling

 $\varphi_s = \varphi_s(t, q_1, \ldots, q_n; q_1, \ldots, q_n) = 0, (s = r + 1, \ldots, m < n).$

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and a relation between the generalized accelerations of the form

$$\frac{\partial \varphi_1}{\partial q_1} \dot{q}_1 + \frac{\partial \varphi_2}{\partial q_2} \dot{q}_2 + \ldots + \frac{\partial \varphi_3}{\partial q_n} \dot{q}_n + (\bullet) = 0, \quad (s = r+1, \ldots, m),$$

the equation of motion is derived as

$$Q_{l} + S_{l} + \lambda_{l} \frac{\partial \varphi_{l}}{\partial q_{l}} + \lambda_{k} \frac{\partial \varphi_{k}}{\partial q_{l}} + \ldots + \lambda_{m} \frac{\partial \varphi_{m}}{\partial q_{l}} = 0, \quad (l = 1, 2, \ldots, n),$$

using the method of Lagrange multipliers. Similarly for an acceleration equation of the form

$$\ddot{q}_1 = b_{s1}\ddot{q}_1 + b_{s2}\ddot{q}_2 + \ldots + b_{s, n-r}\ddot{q}_{n-r} + (*), (s = n-r+1, \ldots, n).$$

the equation of motion is derived as

$$\frac{\partial S}{\partial q_i} - \overline{Q}_i + \mu_1 \frac{\partial q_{r+1}}{\partial q_1} + \mu_2 \frac{\partial \overline{q}_{r+2}}{\partial q_2} + \dots + \mu_{m-r} \frac{\partial q_m}{\partial q_i}, \ (i \text{ as } 1, 2, \dots, n-r).$$

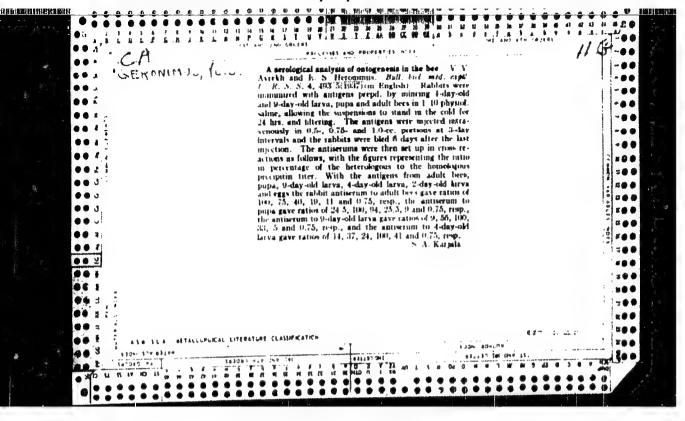
Using a specific example, it is shown that the derived equations give the same results as the Appel! equations. Orig. art. has: 19 formulas.

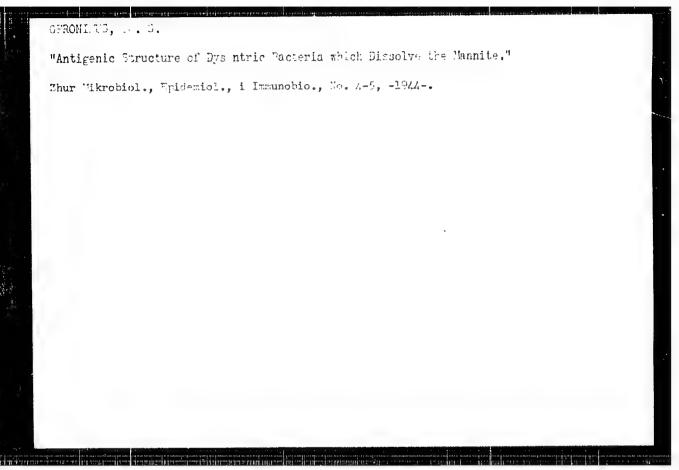
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Card 2/2 BLG





AVREKH, V.V., GERONIMUS, YE.S.

"Vi and O-Antigens in Typhoid Immunity" teo-part article:

- I. "Separation of Vi-Antigen from the Complete Antigens of Typhoid Bacteria," Zhur. Mikrob., Epidem. i Immunobiol., no. 1, pp 33-35, 1947.
- II. "Vi- and O-Antigens in Active and Passive Typhoid Immunity," Zhur. Mikrob., Epidem. i Immunobiol., no. 1,pp 35-38, 1947

State Control Inst. of Vaccines and Serums im. L.A. Tarasevich

	USSR/Medicine - Pneumococci Medicine - Nucleins	Mar/Apr 48				
	"Chemical Nature and Biological Specificity of the Substance Inducing Transformation of Types of Pneumococci," Ye. S. Geronimus, 22 pp					
	"Uspekhi Sovrem Biol" Vol XXV, N	lo 2				
	Describes experiments of M.McCart 1946). Discusses nature of trans Active agent is specific nucleic type.	forming substance.				
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GERGYMUS. Ye.S., zaveduyushchiy otdelem inostramoy literatury.

Abstracts of articles on epidemiology and research on virus hepatitis.

Zhur.mikrobiol.epid.i immun. no.2:90-92 F '53, (MLRA 6:5)

1. Zhurnal mikrobiologii, epidemiologii i immunobiologii.

(Hepatitie, Infectious)

GERONIMUS, Ye.S., saveduyushchiy otdelom.

Abstract of articles on intestinal infections. Zhur. mikrobiol. epid. i immun. no.3:91-95 Mr '53. (MLRA 6:6)

(Intestines--Diseases)

GERONIMUS, Ye.S.; LITINSKIY, Yu.I.; SINAY, G.Ya., professor, zaveduyushchiy; TIMAKOV, V.D., professor, direktor.

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S- and R-forms of Sonne dysentery bacilli and their relationship. Zhur. mikrobiol.epid.i immun. no.8:68-76 Ag '53. (MIRA 6:11)

1. Otdel epidemiologii Instituta epidemiologii i mikrobiologii in. pochetnogo akademika N.F.Gamalei Akademii meditsinskikh nauk SSSR (for Sinay). 2. Institut epidemiologii i mikrobiologii in. pochetnogo akademika N.F.Gamalei Akademii meditsinskikh nauk SSSR (for Timakov). (Dysentery)

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*	GERONIMUS, Ye.S.
	Foreign literature: Abstracts of articles on children's infections. Zhur. mikrobiol.epid.i immun. no.9:88-92 S '53. (MLRA 6:11) (BibliographyChildrenDiseases) (DiseasesChildrenBibliography) (BibliographyInfection) (InfectionBibliography)

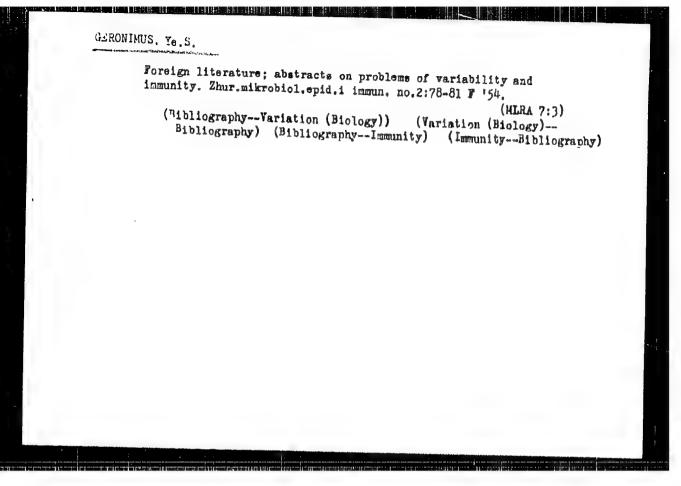
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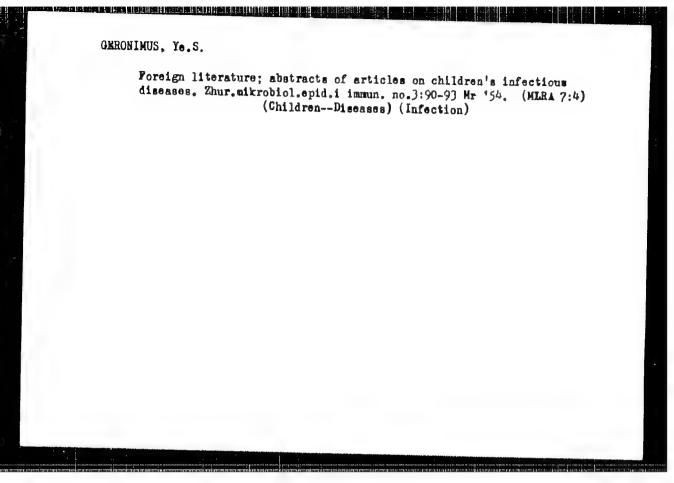
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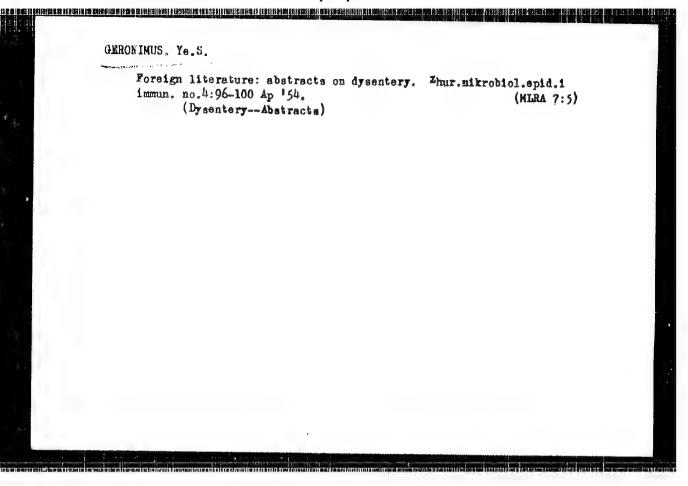
Foreign literature. Research methods, antibiotics. Zhur.mikrobiol.epid.i immun. no.1:81-85 Ja '54.

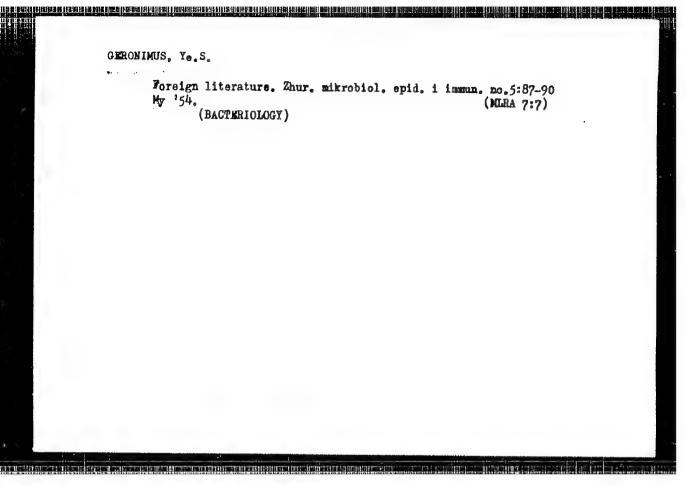
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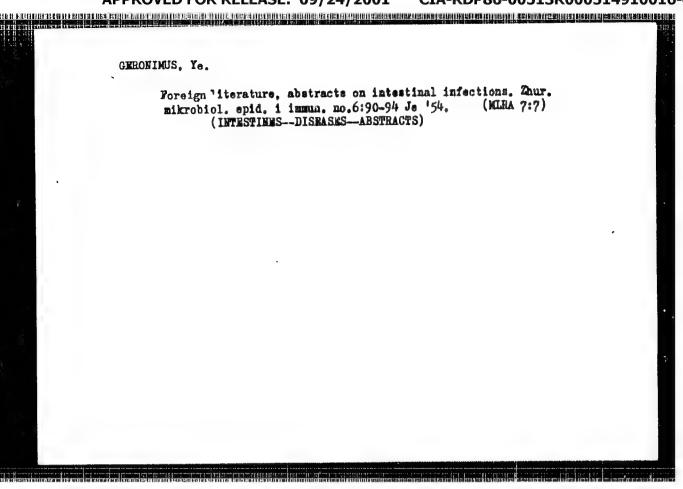
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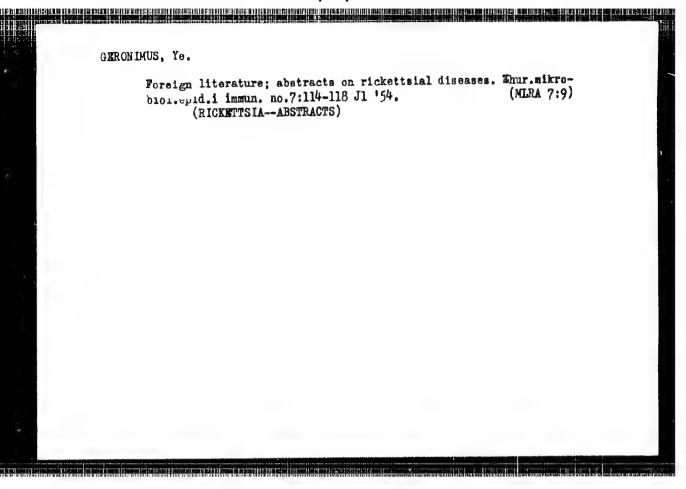












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Author

: Geronimus, Ye. S.

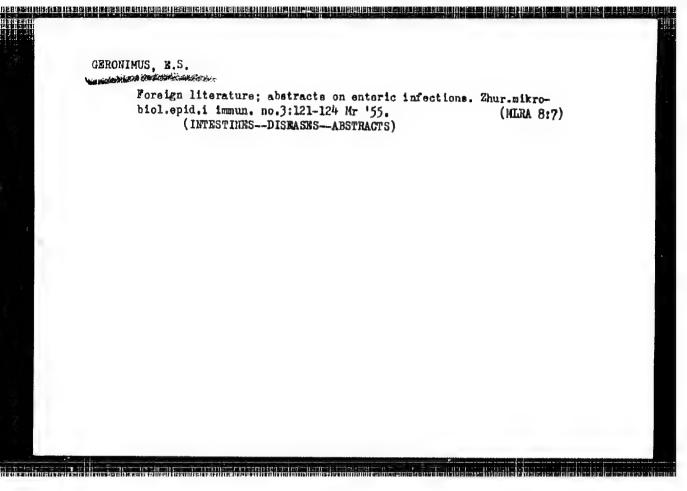
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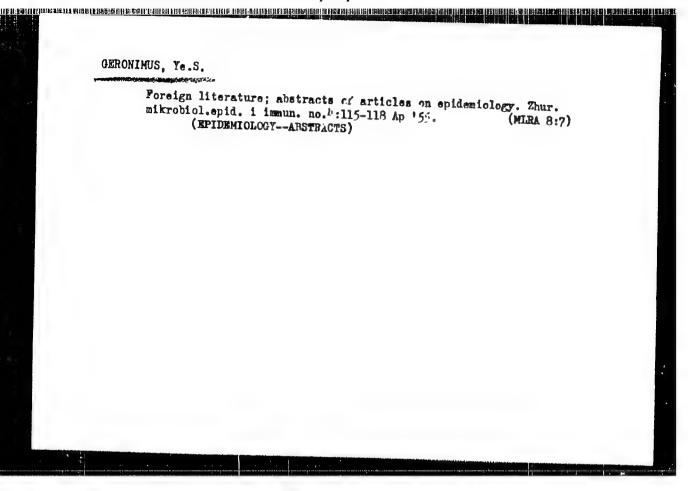
: Foreign publications

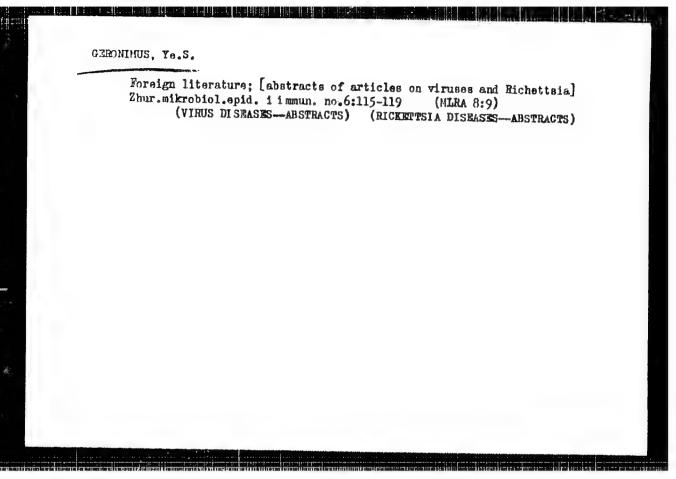
Periodical : Zhur. mikro. epid. i immun. No 2, 123-127, Feb 1955

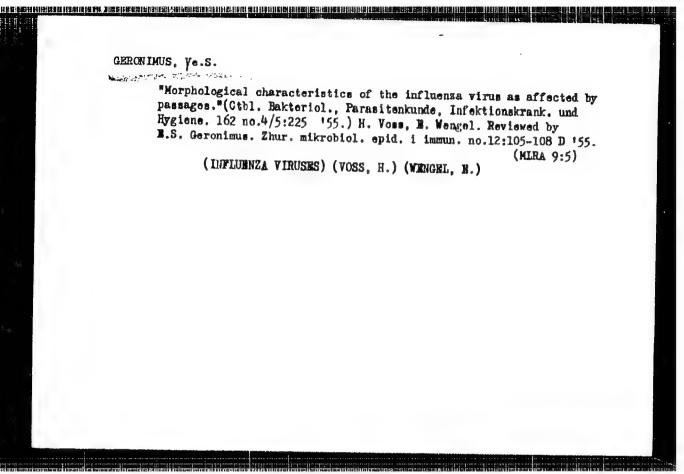
Abstract

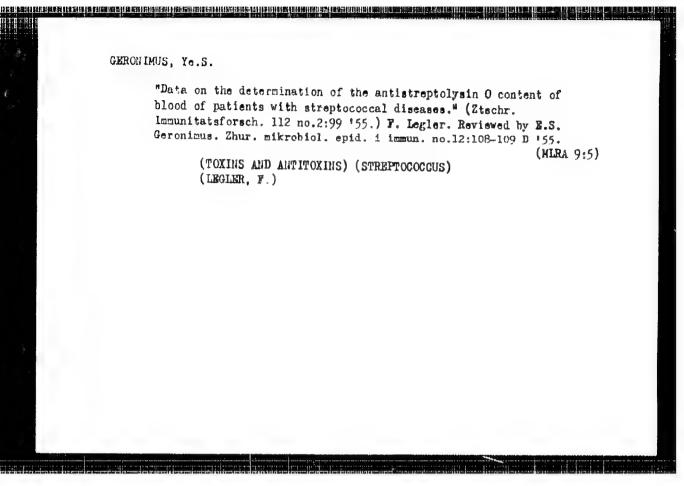
: 14 abstracts of articles published in non-USSR periodicals. The articles abstracted deal with children's infectious diseases.







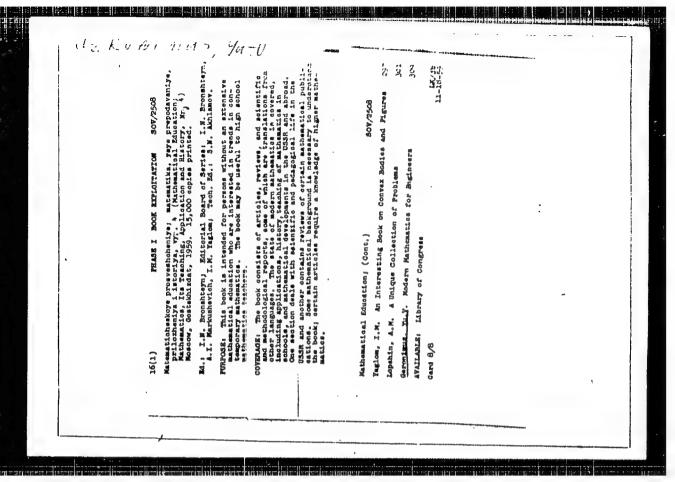




GERONIMUS, Ye.8.

*Experimental study of streptococoal diseases and their aftereffects."
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AUTHORS:

Vinograd, R.E., and Geronimus, Yu.V. (Moscow)

TITLE:

An extrapolation-gradient method of finding the

minimum of a quadratic function

PERIODICAL: Avtomatika i telemekhanika, v. 22, no. 6, 1961, 696 - 710

TEXT: The paper investigates the work of an automatic optimizer searching for the minimum of the function

> $y(x) = ax^2 + bx + c, a > 0$ (1)

(a, b, c are unknown constants) in the presence of random error at the output of measuring device, i.e. when for a given argument x the latter determines

Y(x) = y(x) + z(2)

instead of y(x). If there were no error z, the minimum abscissa

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An extrapolation-gradient ...

for (1) $x_{min} = -b/2a$ could be found by extrapolation from 3 values of y(x) at arbitrary points $x_0 - h$, x_0 , $x_0 + h$ (the number h is called "trial step"). The point x_0 and the "trial step" are to be chosen at random and the transition from x_n to $x_{n\pm 1}$ (called "one cycle of search") is made by measuring the values

$$Y_n^- = Y(x_n - h), \quad Y_n = Y(x_n), \quad Y_n^+ = Y(x_n + h),$$

and determining the "working" step \triangle_n ; then $\mathbf{x}_{n+1} = \mathbf{x}_n + \triangle_n$. A provisional method of determining \triangle is devised which turns out to be useless since the process is divergent. To avoid divergence one can choose some "protective number" $\mathbf{k} > 0$ and make \triangle_n depend on relation of \mathbf{y}_n^- etc. to \mathbf{k} . There are four possible variants; the best one is

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An extrapolation-gradient ...

$$x_{n+1} = x_n + \frac{h}{2} \frac{Y_n^- - Y_n^+}{k}, \quad \text{if } Y_n^- + Y_n^+ - 2Y_n < k,$$

$$x_{n+1} = x_n + \frac{h}{2} \frac{Y_n^- - Y_n^+}{Y_n^- + Y_n^+ - 2Y_n}, \quad \text{if } Y_n^- + Y_n^+ - 2Y_n \geqslant k.$$
(5)

Consisting in a combination of extrapolation method and gradient method which is the one analyzed in the paper. Chance values of the argument \mathbf{x}_1 , \mathbf{x}_2 ... obtained by (5) lead to chance values of \mathbf{y} : \mathbf{y}_1 , \mathbf{y}_2 ; in addition there are values

$$y_n^{\pm} = y(x_n \pm h)$$

in every cycle. Optimization should make the quantities $y_n^t = y_n - y_{min}$, $y_n^{t\pm} = y_n^{\pm} - y_{min}$ tend to 0. The quantity Card 3/5

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An extrapolation-gradient ...

$$u_n = \frac{1}{3} (y_n' - y_n' + y_n')$$

is chosen as the measure of their common deviation from 0. The problems are: Determination of mathematical expectations \bar{u}_n and dispersions Du_n , the limits $U=\lim \bar{u}_n$ and $D=\lim Du_n$ $(n\to\infty)$ etc. D is called the established dispersion and U the established error. The results are: The sequences \bar{u}_n and Du_n converge as geometrical progressions with respective denominators A and L; A is called the "convergence coefficient". The region of convergence of the process (shaded area on Fig.1) does not contain some values of k near 0, so that one cannot choose the protective number to be arbitrary small, without taking into account the value of h. Simultaneous decrease of convergence coefficient A and established error U is impossible; if h and k are so chosen that $A\to 0$, $U\to\infty$; if $U\to 0$, $A\to 1$. There is an optimum curve in the region of convergence, having the property that one can pass from any

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An extrapolation-gradient ...

point of the region to a point on the curve in such a manner that one of the numbers A, U remains constant and the other diminishes. The authors thank A. Fel'dbaum for formulating the problem and discussing the results. There are 6 figures and 2 Soviet-bloc references.

SUBMITTED: February 18, 1961

Fig. 1. Region of convergence and the optimum curve:

Legend: 1 - Optimum curve; $2 - k = 2ah^2$.

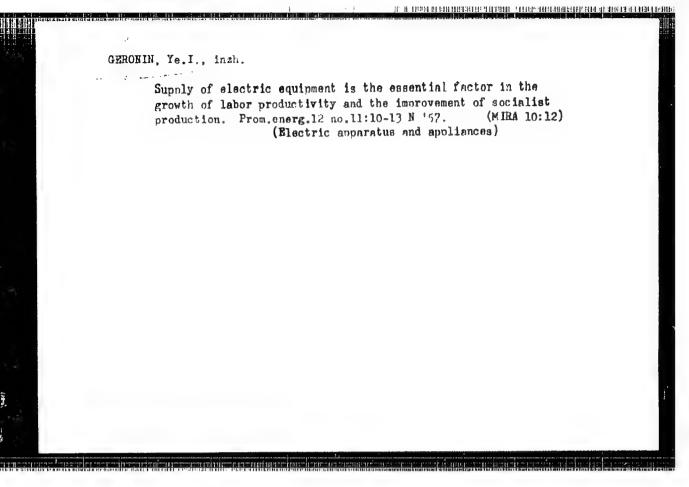
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Рис. 1 Область еходимости и оптимальная кривая: I — оптимальная криваи, 2 — $k = 2ah^2$

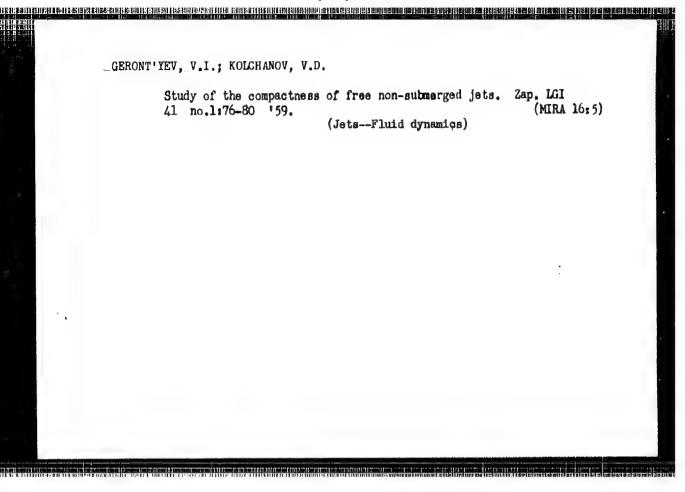
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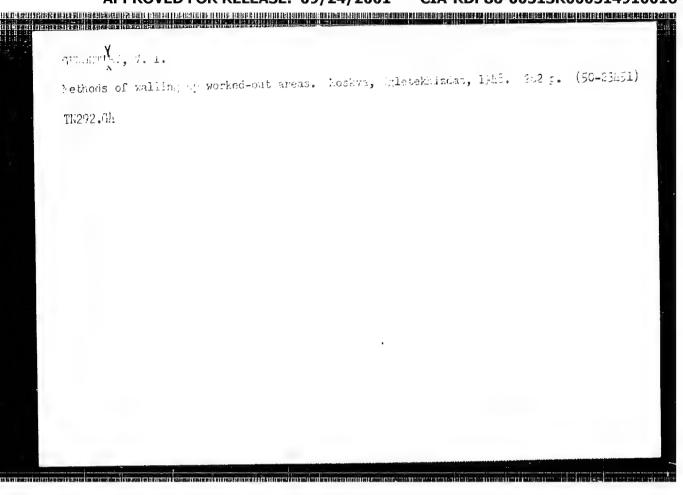


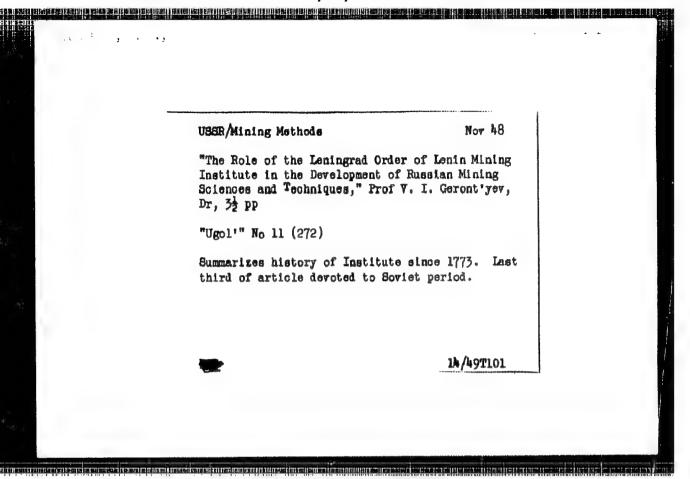
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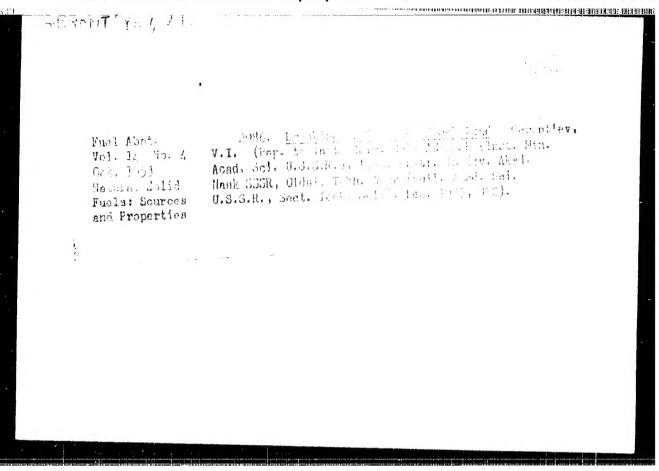
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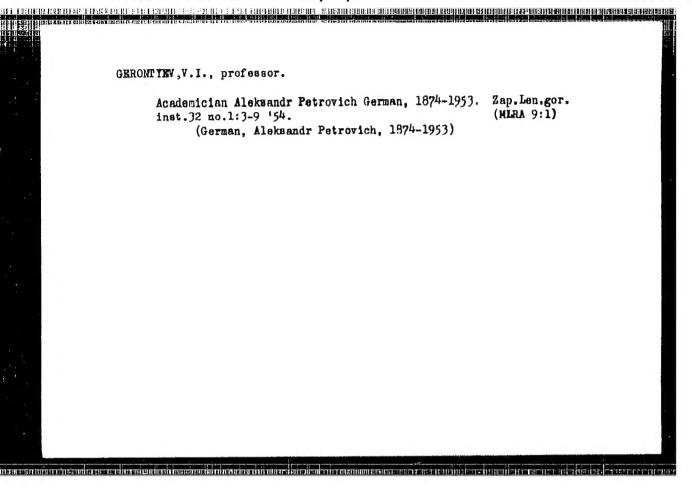




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In memory of Professor Levenson. Gor. Zhur. no.9:60 S '55.

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